

**Problem 12.22)**

- |  | Real | Imaginary |
|--|------|-----------|
| a) $\alpha \cdot \beta = (\alpha' + i\alpha'') \cdot (\beta' + i\beta'') = \underbrace{(\alpha' \cdot \beta' - \alpha'' \cdot \beta'')}_{0} + i(\alpha' \cdot \beta'' + \alpha'' \cdot \beta').$   |      |           |
| b) $\alpha \times \beta = (\alpha' + i\alpha'') \times (\beta' + i\beta'') = (\alpha' \times \beta' - \alpha'' \times \beta'') + i(\alpha' \times \beta'' + \alpha'' \times \beta').$  |      |           |
| c) $\gamma \times \gamma = (\gamma' + i\gamma'') \times (\gamma' + i\gamma'') = \cancel{\underbrace{\gamma' \times \gamma'}_0} - \cancel{\underbrace{\gamma'' \times \gamma''}_0} + i(\gamma' \times \gamma'' + \gamma'' \times \gamma') = 0 + i0.$  |      |           |
| d) $\begin{aligned} \alpha \cdot (\beta \times \gamma) &= (\alpha' + i\alpha'') \cdot [(\beta' + i\beta'') \times (\gamma' + i\gamma'')] \\ &= (\alpha' + i\alpha'') \cdot [(\beta' \times \gamma' - \beta'' \times \gamma'') + i(\beta' \times \gamma'' + \beta'' \times \gamma')] \\ &= [\alpha' \cdot (\beta' \times \gamma' - \beta'' \times \gamma'') - \alpha'' \cdot (\beta' \times \gamma'' + \beta'' \times \gamma')] \quad \leftarrow \text{Real} \\ &\quad + i[\alpha' \cdot (\beta' \times \gamma'' + \beta'' \times \gamma') + \alpha'' \cdot (\beta' \times \gamma' - \beta'' \times \gamma')]. \quad \leftarrow \text{Imaginary} \end{aligned}$ |      |           |
-